15CS653

Sixth Semester B.E. Degree Examination, Jan./Feb. 2023 **Operations Research**

CBCS SCHEWE

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

Define Operation Research. 1 a.

(04 Marks)

Discuss basic components of LP model.

(04 Marks)

A computer company manufactures laptops and desktops that fetch total profit of Rs.700/and 500/- per unit respectively. Each unit of laptop takes 4 hours of assembly time and 2 hours of testing time while each unit of desktop requires 3 hours of assembly time and 1 hour for testing. In a given month the total number of hours available for assembly is 210 hours and for inspection is 90 hours. Formulate the problem as LPP in such a way that the total profit is maximum. (08 Marks)

OR

Describe the steps involved in the formulation of LPP.

(04 Marks)

Explain the terms: (i) Feasible solution (ii) unbounded solution

(04 Marks)

A company produces two types of leather belts A and B and their profits are 40 and 30 rupees respectively. Each belt of type A requires twice as much a time as required for B. Company can produce 1000 belts per day. Leather is sufficient only for 800 belts per day. Belt A requires fancy buckles, there are only 400 buckles per day. For B only 700 buckles per day are available. How should the company manufacturers the 2 types of belts in order to maximize overall profit? Solve using graphical method. (08 Marks)

Module-2

- Define with example: (i) Slack variable (ii) Surplus variable (iii) Basic feasible 3 solution. (06 Marks)
 - b. Solve the following LPP using simplex method:

$$Z_{\text{max}} = 3x_1 + 2x_2$$

Subjected to $x_1 + x_2 \le 40$ $x_1 - x_2 \le 20$ where $x_1, x_2 \ge 0$

$$x_1 - x_2 \le 20$$

where
$$x_1, x_2 \ge 0$$

(10 Marks)

a. Solve the following LPP using Big M method:

 $Minimize z = 2x_1 + 3x_2$

Subjected to constraints $x_1 + 2x_2 \le 4$

$$x_1 + x_2 = 3$$
 and x_1 and $x_2 \ge 0$

$$x_1$$
 and $x_2 \ge 0$

(10 Marks)

Explain briefly two phase method.

(06 Marks)

Module-3

Explain the procedure of dual simplex method. 5 a.

(06 Marks)

Use dual simplex method to solve the following LPP: b.

$$Minimize z = 2x_1 + x_2 + 3x_3$$

Subjected to
$$x_1 - 2x_2 + x_3 \ge 4$$

$$2x_1 + x_2 + x_3 \le 8$$
 and $x_1 - x_3 \ge 0$ with all variables non negative. (10 Marks)

OR

- 6 a. Explain briefly: (i) Formulation of dual linear programming problem.
 - (ii) Unrestricted variables.

(06 Marks)

b. The dual simplex method to solve the following problem:

Maximize $z = -2x_1 - 3x_2$

Subjected to $x_1 + x_2 \ge 2$

$$2x_1 + x_2 \le 10$$

$$x_1 + x_2 \le 8$$

with x_1 and x_2 non negative.

(10 Marks)

Module-4

7 a. Explain North-West corner method with an example.

(06 Marks)

b. Using Vogel's Approximation Method (VAM), solve the following transportation problem:

Demand

	D_1	D_2	D_3	<i>y</i> • .
O_1	2	7	4	5
O_1 O_2 O_3 O_4	3	3	8	8
O_3	5 <	4	7	7
O_4	1	6	2	14
	8	8	18	0

(10 Marks)

OF

a. Explain different types of assignment problems.

(06 Marks)

b. Four new computers (C₁, C₂, C₃, C₄) are to be installed in a computer center. There are 5 vacant places (A, B, C, D and E) available. Because of limited space C₂ cannot be placed at C. and C₃ cannot be placed at A. The assignment cost of the computers to the places is given below. Find the optimal assignment.

	A	В	C	D	E
C_1	4	6	10	5	6
\mathbb{C}_2	7	4	-	5	4
C_3	•	6	9	6	2
C ₄	9	3	7	2	3

(10 Marks)

Module-5

9 a. Explain two person zero-sum game and non zero-sum game with example.

(06 Marks)

b. Solve the following game whose pay off matrix is,

Player B
$$\begin{array}{c|c}
 & \text{Player B} \\
\hline
 & 3 & -2 \\
 & 2 & 5
\end{array}$$

(10 Marks)

OR

10 a. List the applications of game theory.

(04 Marks)

b. Explain min-max and max-min principle.

(04 Marks)

c. Distinguish between pure strategy and mixed stratergy.

(04 Marks)

d. Explain the concept of dominance.

(04 Marks)

2 of 2